

PHYS 4A – Spring 2024 – Midterm 2

Question:	1	2	3	4	Total
Points:	6	8	8	8	30
Bonus Points:	2	2	0	0	4
Score:					

Remember to pay attention to significant figures and don't get lost in long calculations. The answers are usually only a few lines.

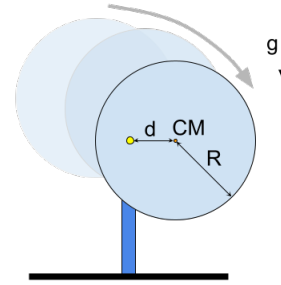
- There is a truck filled with water and it's at rest. Suddenly the valve for the tank is opened and water starts flowing out horizontally at a rate of 5.00 kg/s with a speed of 20.0 m/s relative to the truck.



*Hint: Use rocket equations*

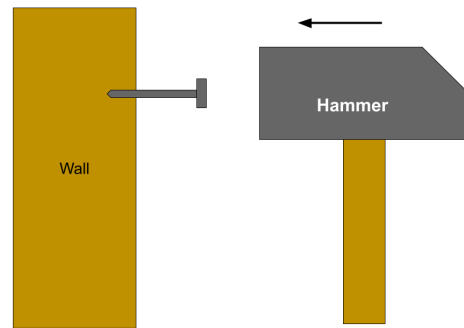
- (3 points) What is the thrust force created by the water jet on the truck?
- (3 points) Assuming mass flow rate and speed is constant, what is the final velocity of the truck after  $2.00 \times 10^3$  kg of water have been ejected?
- (2 points (bonus)) Is the acceleration of the truck constant? If not, when is acceleration highest and when is it lowest?

2. A uniform disc of mass  $m$  and radius  $R$  is attached to a vertical pole with a frictionless hinge a distance  $d$  away from its center and allowed to rotate freely subject to gravity. The **lowest** angular velocity observed is  $\omega_L$ . Ignore air friction.  $I_{CM} = mR^2/2$



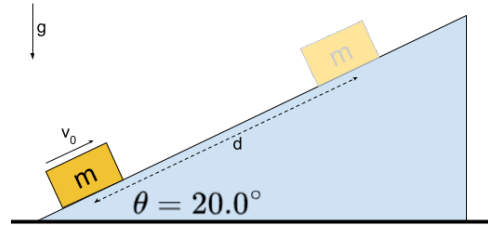
- (a) (2 points) At what positions will  $\omega_L$  and  $\omega_H$  be observed respectively? (Describe as the position of the *center of mass* CM with respect to the hinge).
- (b) (2 points) What is the difference in potential energy between the positions corresponding to  $\omega_L$  and  $\omega_H$
- (c) (4 points) Calculate the expression for  $\omega_H$  in terms of  $d, R, g, \omega_L$ .
- (d) (2 points (bonus)) Show that if  $d = 0$  then  $\omega_L = \omega_H$ . Explain why that's the case.

3. When hammering a nail into wood, the worker gives the hammer an initial speed of  $v_i = 10.0 \text{ m/s}$  just before it hits the nail. The hammer drives the nail in by  $d = 1.5 \text{ cm}$  and comes to a complete stop. The nail experiences a resistive force of  $F_R = 1.20 \text{ kN}$  to penetrate the wood.



- (a) (2 points) What is the total work done on the nail?
- (b) (2 points) Is momentum conserved for the hammer? Explain.
- (c) (4 points) Calculate the mass of the hammer assuming all the energy is transferred to the nail.

4. An object of mass  $m = 1.00 \text{ kg}$  is given an initial velocity of  $v_0 = 8.00 \text{ m/s}$  on an incline with an angle  $\theta = 20.0^\circ$ . The object comes to rest after travelling a distance  $d = 7.00 \text{ m}$  on the incline due to friction.



- (a) (2 points) Draw a box within which energy is conserved and calculate the initial energy of the system.
- (b) (2 points) Calculate the amount of non-conservative work done.
- (c) (4 points) Calculate the coefficient of friction  $\mu_k$ .