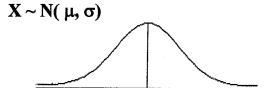
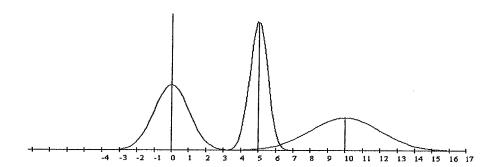
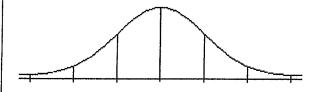
## CHAPTER 6: THE NORMAL PROBABILITY DISTRIBUTION Exploring the Normal Probability Distribution





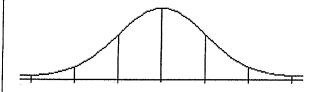
- a. The normal distributions above have means  $\mu = 5$ ,  $\mu = 10$  and  $\mu = 0$ . Identify which graph has which mean.
- b. The normal distributions above have standard deviations of  $\sigma = 0.5$ ,  $\sigma = 1$  and  $\sigma = 2$ . Identify graph has which standard deviation.

The following are true for ANY normal probability distribution:



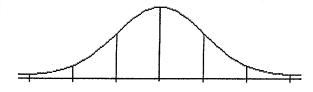
$$P(\mu - \sigma < X < \mu + \sigma) = \underline{\hspace{1cm}}$$

The probability for the interval within  $\pm 1$  standard deviations from the mean ( $\mu \pm 1\sigma$ ) is \_\_\_\_\_



$$P(\mu - 2\sigma < X < \mu + 2\sigma) = \underline{\hspace{1cm}}$$

The probability for the interval within  $\pm 2$  standard deviations from the mean  $(\mu \pm 2\sigma)$  is \_\_\_\_\_



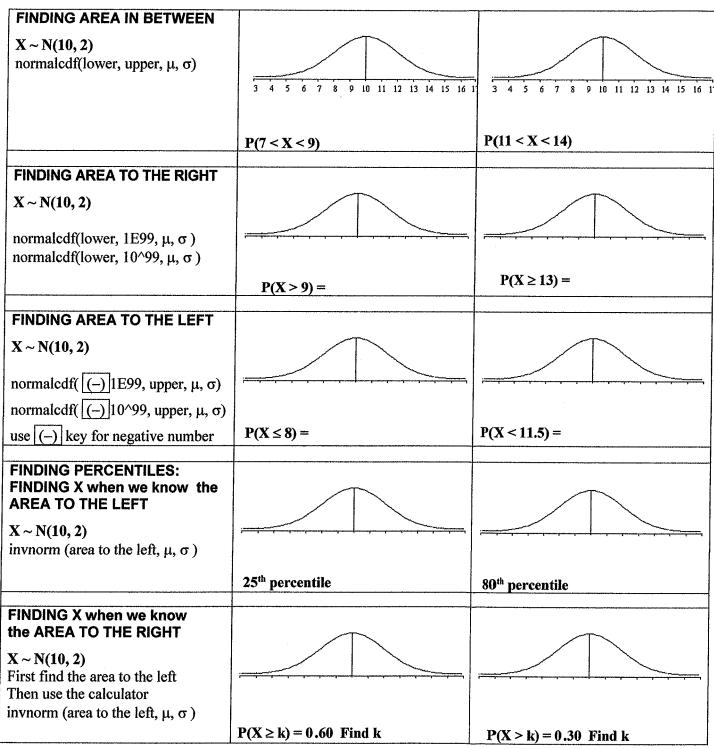
$$P(\mu -3\sigma < X < \mu +3\sigma) = \underline{\hspace{1cm}}$$

The probability for the interval within  $\pm 3$  standard deviations from the mean  $(\mu \pm 3\sigma)$  is

#### **CHAPTER 6: THE NORMAL PROBABILITY DISTRIBUTION: Calculating Probabilities**

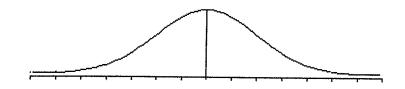
- Shade the area representing the probability.
- Label the value of the mean μ and the X values along the horizontal axis
- Label area above or inside the graph.
- Use your calculator: 2<sup>nd</sup> Distr normaldef to find the probabilities if given X or use 2<sup>nd</sup> Distr invnorm to find X if given the probability (invnorm requires input of area to the **left**)
- Write the answer as a mathematical probability statement using correct notation.

A botanist is studying the amount of time it takes for seeds to germinate (sprout) for certain type of plant. Suppose that the germination time is normally distributed with a mean (average) of 10 days with standard deviation 2 days. X = germination time for one seed



# CHAPTER 6: THE NORMAL PROBABILITY DISTRIBUTION: Calculating Probabilities FINDING TWO X VALUES WHEN WE KNOW THE AREA IN THE MIDDLE

 $X \sim N(10,2)$ 

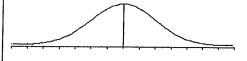


The middle 90% of values are between and In context of the example stated on page 2 for seed germination time of plants X~N(10,2) days,

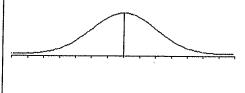
The middle 90% of seed take between \_\_\_\_\_ and \_\_\_\_ days to sprout (germinate).

 $P(c \le X \le d) = 0.90$  Find c and d:

1. First figure out the area to the left of the lower bound.



2. Then figure out area to the left of the upper bound



3. Then use the calculator with invnorm TWICE to find the lower and upper bounds:

lower bound =

area to left of

$$\mathit{invnorm}igg( egin{area to left of \\ \mathit{lower bound} \end{matrix}, \mu, \sigma igg)$$

upper bound =

invnorm 
$$\begin{cases} area \text{ to left of} \\ upper \text{ bound} \end{cases}$$
,  $\mu$ ,  $\sigma$ 

## CHAPTER 6: THE NORMAL PROBABILITY DISTRIBUTION Exploring Connections between Percentiles and Z-Scores

Two swimmers, Angie and Beth, from different wim teams want to compare who had the fastest time for the 50 meter freestyle race when compared relative to the other swimmers on her own team. Suppose we also know that times for each team follow a normal distribution.

Dean, S., & Illowsky, B. OpenStax Introductor Statistics Download for free at https://openstax.org/details/introductory-statistics

Swimmer	Swimmer's Time	Team Mean Time	Team Standard Deviation
Angie	26.2	27.2	0.8
Beth	27.3	30.1	1.4

Which swimmer's time would be considered better (Angie or Beth) when each is compared relative to the other swimmers on her own team?

Calculate and con	mpare <b>Z-scores</b> (we did	this in chapter 2; chapter 6 re-examines this co
Angie		Beth
Compare percent	iles for Angie and Beth	by calculating probabilities using their actual G
Angie: Find P(X <	$\leq 26.2$ ) for X~N(27.2, 0	Beth: Find $P(Y \le 27.3)$ using $Y \sim N(30.3)$
		h by calculating probabilities using their z-score
Angie: Find P(Z <	$(-1.25)$ using $Z \sim N(0)$	9, 1) Beth: Find $P(Z < -2)$ using $Z \sim N(0, 1)$
		······································

distribution,  $Z \sim N(0, 1)$ 

### **CHAPTER 6: THE NORMAL PROBABILITY DISTRIBUTION: PRACTICE**

- Draw the graph and label all pertinent values.
- $\bullet$  Label the value of the mean  $\mu$  and the X values along the horizontal axis
- Label areas above or inside the graph.
- Use your calculator to find the requested values. Write your calculator commands.
- Write the answer as a mathematical probability statement using correct notation.

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<b>PRACTICE EXAMPLE N:</b> In California, the wine and fruit industries invest significant resources study of growing grapes in order to improve crop yield and quality. Suppose that a certain type of grape, when ripe, has diameter that is normally distributed with a me 1.8 cm with a standard deviation of 0.3 cm.
a. Find the probability that a randomly selected grape has diameter more than 2.2 cm
b. Find the probability that a randomly selected grape has diameter less than 1.6 cm.
c. The middle 80% of this type of grapes have diameters between and cm.
d.Find the IQR (Interquartile Range) of diameters for this type of grape.
e. The largest 15% of grapes have diameters of at least cm.

- f. Find the probability that a randomly selected grape has diameter between 1.5 and  $2.0\ cm$ using each method as instructed below:
  - (i) Use X~N(1.8, 0.3) when using normalcdf on your calculator
  - (ii) Find z-scores for x = 1.5 and x = 2.0 and use  $Z \sim N(0,1)$  standard normal distribution when using normalcdf on your calculator